

### **Tables for the Kansas Mathematics Standards**

Below you will find the tables found in the Kansas Mathematics Standards. Click on the table you would like to view and you will be redirected to the correct page in the document.

<u>Table 1</u>
<u>Table 2</u>
Table 3
Table 4
Table 5

#### Table 1

#### **Common Addition and Subtraction Situations** (pg 88 in CCSS)

Shading taken from OA progression

	Result Unknown	Change Unknown	Start Unknown
Add to	Two bunnies sat on the grass. Three more bunnies hopped there. How many bunnies are on the grass now? 2 + 3 = ?	Two bunnies were sitting on the grass. Some more bunnies hopped there. Then there were five bunnies. How many bunnies hopped over to the first two? 2+?=5	Some bunnies were sitting on the grass. Three more bunnies hopped there. Then there were five bunnies. How many bunnies were on the grass before? ? $+3 = 5$
Taken from	Five apples were on the table. I ate two apples. How many apples are on the table now? $5-2=?$	Five apples were on the table. I ate some apples. Then there were three apples. How many apples did I eat? 5-?=3	Some apples were on the table. I ate two apples. Then there were three apples. How many apples were on the table before? ? $-2 = 3$
	Total Unknown	Addond Unknown	Both Addends Linknown <sup>1</sup>
Put Together/ Take Apart <sup>2</sup>	Three red apples and two green apples are on the table. How many apples are on the table? 3 + 2 = ?	Five apples are on the table. Three are red and the rest are green. How many apples are green? 3+?=5, 5-3=?	Grandma has five flowers. How many can she put in her red vase and how many in her blue vase? 5 = 0 + 5, $5 = 5 + 05 = 1 + 4$ , $5 = 4 + 15 = 2 + 3$ , $5 = 3 + 2$
	Difference Unknown	Bigger Unknown	Smaller Unknown
Compare <sup>3</sup>	("How many more?" version): Lucy has two apples. Julie has five apples. How many more apples does Julie have than Lucy? ("How many fewer?" version):	(Version with "more"): Julie has three more apples than Lucy. Lucy has two apples. How many apples does Julie have?	(Version with "more"): Julie has three more apples than Lucy. Julie has five apples. How many apples does Lucy have? (Version with "fewer"):
	Lucy has two apples. Julie has five apples. How many fewer apples does Lucy have than Julie? 2+?=5, 5-2=?	Lucy has 3 fewer apples than Julie. Lucy has two apples. How many apples does Julie have? 2+3=?, $3+2=?$	Lucy has 3 fewer apples than Jul 2. Julie has five apples. How many apples does Lucy have? 5-3=?, $?+3=5$

Blue shading indicates the four Kindergarten problem subtypes. Students in grades 1 and 2 work with all subtypes and variants (blue and green). Yellow indicates problems that are the difficult four problem subtypes or variants that students in Grade 1 work with but do not need to master until Grade 2.

<sup>&</sup>lt;sup>1</sup>These take apart situations can be used to show all the decompositions of a given number. The associated equations, which have the total on the left of the equal sign, help children understand that the = sign does not always mean makes or results in but always does mean is the same number as.

<sup>&</sup>lt;sup>2</sup>Either addend can be unknown, so there are three variations of these problem situations. Both Addends Unknown is a productive extension of this basic situation, especially for small numbers less than or equal to 10.

<sup>&</sup>lt;sup>3</sup>For the Bigger Unknown or Smaller Unknown situations, one version directs the correct operation (the version using more for the bigger unknown and using less for the smaller unknown). The other versions are more difficult.

#### Table 2

#### **Common Multiplication and Division Situations** (pg 89 in CCSS)

Grade level identification of introduction of problems taken from OA progression

Unknown Product		Group Size Unknown ("How many in each group?" Division)	Number of Groups Unknown ("How many groups?" Division)
	$3 \times 6 = ?$	$3 \times ? = 18, \qquad 18 \div 3 = ?$	$? \times 6 = 18, \qquad 18 \div 6 = ?$
	There are 3 bags with 6 plums in each bag. How many plums are there in all?	If 18 plums are shared equally into 3 bags, then how many plums will be in each bag?	If 18 plums are to be packed 6 to a bag, then how many bags are needed?
Equal Groups	Measurement example. You need 3 lengths of string, each 6 inches long. How much string will you need altogether?	Measurement example. You have 18 inches of string, which you will cut into 3 equal pieces. How long will each piece of string be?	Measurement example. You have 18 inches of string, which you will cut into pieces that are 6 inches long. How many pieces of string will you have?
	There are 3 rows of apples with 6 apples in each row. How many apples are there?	If 18 apples are arranged into 3 equal rows, how many apples will be in each row?	If 18 apples are arranged into equal rows of 6 apples, how many rows will there be?
Arrays⁴, Area⁵	<i>Area example.</i> What is the area of a 3 cm by 6 cm rectangle?	Area example. A rectangle has area 18 square centimeters. If one side is 3 cm long, how long is a side next to it?	Area example. A rectangle has area 18 square centimeters. If one side is 6 cm long, how long is a side next to it?
	A blue hat costs \$6. A red hat costs 3 times as much as the blue hat. How much does the red hat cost?	A red hat costs \$18 and that is 3 times as much as a blue hat costs. How much does a blue hat cost? Measurement example.	A red hat costs \$18 and a blue hat costs \$6. How many times as much does the red hat cost as the blue hat?
Compare	Measurement example. A rubber band is 6 cm long. How long will the rubber band be when it is stretched to be 3 times as long?	A rubber band is stretched to be 18 cm long and that is 3 times as long as it was at first. How long was the rubber band at first?	Measurement example. A rubber band was 6 cm long at first. Now it is stretched to be 18 cm long. How many times as long is the rubber band now as it was at first?
General	$a \times b = ?$	$a \times ? = p and p \div a = ?$	$? \times b = p \text{ and } p \div b = ?$

Multiplicative compare problems appear first in Grade 4 (green), with whole number values and with the "times as much" language from the table. In Grade 5, unit fractions language such as "one third as much" may be used. Multiplying and unit language change the subject of the comparing sentence ("A red hat costs n times as much as the blue hat" results in the same comparison as "A blue hat is  $\frac{1}{n}$  times as much as the red hat" but has a different subject.)

## Table 3Fundamental Properties of Number and Operations

Name of Property	Representation of Property	Example of Property, Using Real Numbers		
Properties of Addition				
Associative	(a+b) + c = a + (b+c)	(78 + 25) + 75 = 78 + (25 + 75)		
Commutative	a+b=b+a	2 + 98 = 98 + 2		
Additive Identity	a + 0 = a  and  0 + a = a	9875 + 0 = 9875		
Additive Inverse	For every real number $a$ , there is a real number $-a$ such that a + -a = -a + a = 0	-47 + 47 = 0		
Properties of Multiplication				
Associative	$(a \times b) \times c = a \times (b \times c)$	$(32 \times 5) \times 2 = 32 \times (5 \times 2)$		
Commutative	$a \times b = b \times a$	$10 \times 38 = 38 \times 10$		
Multiplicative Identity	$a \times 1 = a \text{ and } 1 \times a = a$	$387 \times 1 = 387$		
Multiplicative Inverse	For every real number $a, a \neq 0$ , there is a real number $\frac{1}{a}$ such that $a \times \frac{1}{a} = \frac{1}{a} \times a = 1$	$\frac{8}{3} \times \frac{3}{8} = 1$		
Distributive Property of Multiplication over Addition				
Distributive	$a \times (b + c) = a \times b + a \times c$	$7 \times (50 + 2) = 7 \times 50 + 7 \times 2$		

(Variables a, b, and c represent real numbers.)

Excerpt from Developing Essential Understanding of Algebraic Thinking, grades 3-5 p. 16-17

# Table 4Properties of Equality

Name of Property	Representation of Property	Example of property
Reflexive Property of Equality	a = a	3,245 = 3,245
Symmetric Property of Equality	If $a + b$ , then $b = a$	2 + 98 = 90 + 10, then $90 + 10 = 2 + 98$
Transitive Property of Equality	If $a = b$ and $b = c$ , then $a = c$	<i>If</i> 2 + 98 = 90 + 10 <i>and</i> 90 + 10 = 52 + 48 <i>then</i> 2 + 98 = 52 + 48
Addition Property of Equality	If $a + b$ , then $a + c = b + c$	If $\frac{1}{2} = \frac{2}{4}$ , then $\frac{1}{2} + \frac{3}{5} = \frac{2}{4} + \frac{3}{5}$
Subtraction Property of Equality	If $a = b$ , then $a - c = b - c$	If $\frac{1}{2} = \frac{2}{4}$ , then $\frac{1}{2} - \frac{1}{5} = \frac{2}{4} - \frac{1}{5}$
Multiplication Property of Equality	If $a = b$ , then $a \times c = b \times c$	If $\frac{1}{2} = \frac{2}{4}$ , then $\frac{1}{2} \times \frac{1}{5} = \frac{2}{4} \times \frac{1}{5}$
Division Property of Equality	If $a = b$ and $c \neq 0$ , then $a \div c = b \div c$	<i>If</i> $\frac{1}{2} = \frac{2}{4}$ , then $\frac{1}{2} \div \frac{1}{5} = \frac{2}{4} \div \frac{1}{5}$
Substitution Property of Equality	If $a = b$ , then $b$ may be substituted for $a$ in any expression containing $a$ .	If 20 = 10 + 10 then 90 + 20 = 90 + (10 + 10)

(Variables a, b, and c can represent any number in the rational, real, or complex number systems.)

### Table 5 TABLE 5: Properties of Inequality

Exactly one of the following is true: a < b, a = b, a > b. If a > b and b > c then a > c. If a > b, then b < a. If a > b, then -a < -b. If a > b, then  $a \pm c > b \pm c$ . If a > b and c > 0, then  $a \times c > b \times c$ . If a > b and c < 0, then  $a \times c < b \times c$ . If a > b and c < 0, then  $a \pm c > b \pm c$ . If a > b and c < 0, then  $a \pm c > b \pm c$ . If a > b and c < 0, then  $a \pm c > b \pm c$ . If a > b and c < 0, then  $a \pm c > b \pm c$ .

Here a, b, and c stand for arbitrary numbers in the rational or real number systems.